

# NA01 — Number System & Simplification

 Numerical Ability – NA01

AFCAT Level

☆ Low Priority

✦ **AFCAT Focus:** NA01 tests **number types** (prime, composite, HCF, LCM), **BODMAS simplification**, and **recurring decimals**. AFCAT questions are direct – typically 1–2 per paper. Master  $HCF \times LCM = \text{Product}$ , and the BODMAS order. Average students can score full marks here with formula memorisation alone.

## 1. Types of Numbers

FIG 1.1 — NUMBER SYSTEM AT A GLANCE

 **RATIONAL NUMBERS** (can write as  $p/q$ )

**Natural:** 1, 2, 3, 4... (no zero)

**Whole:** 0, 1, 2, 3... (includes zero)

**Integers:** ...-2, -1, 0, 1, 2... (no fractions)

**Terminating decimals:** 0.5, 1.25, 0.75

**Recurring decimals:** 0.333..., 0.142857...

⚡ Natural  $\subset$  Whole  $\subset$  Integer  $\subset$  Rational

 **IRRATIONAL NUMBERS** (cannot write as  $p/q$ )

Non-terminating, non-recurring decimals

**Examples:**  $\sqrt{2}$ ,  $\sqrt{3}$ ,  $\pi$ ,  $e$

$\sqrt{(\text{perfect square})} = \text{Rational}$  — e.g.  $\sqrt{4} = 2 \checkmark$

$\sqrt{(\text{non-perfect square})} = \text{Irrational}$  — e.g.  $\sqrt{2} \times$

Rational + Irrational = **Irrational**

$\pi = 3.14159...$   $\sqrt{2} = 1.41421...$   $e = 2.71828...$

**Topic A****Number Types – Complete Reference**

Direct AFCAT Facts

**Natural**

Counting numbers: 1, 2, 3, 4, 5... Does NOT include 0. Also called positive integers.

**Whole**

Natural numbers + zero: 0, 1, 2, 3, 4... Whole numbers include 0; natural numbers do not.

**Integer**

All whole numbers + negative numbers: ..., -3, -2, -1, 0, 1, 2, 3... No fractions or decimals.

**Rational**

Any number expressible as  $\frac{p}{q}$  where  $q \neq 0$ . Includes integers, fractions, terminating & recurring decimals. E.g.  $\frac{3}{4}$ , -2, 0.5, 0.333

**Irrational**

Cannot be written as  $\frac{p}{q}$ . Non-terminating, non-recurring decimals. E.g.  $\sqrt{2}$ ,  $\sqrt{3}$ ,  $\pi$ ,  $e$ .  $\sqrt{(\text{perfect square})}$  is rational.

**Prime**

Exactly 2 factors: 1 and itself. Smallest prime = 2 (only even prime). Primes up to 50: 2,3,5,7,11,13,17,19,23,29,31,37,41,43,47. Note: 1 is NOT prime.

**Composite**

More than 2 factors. Smallest composite = 4. All even numbers  $> 2$  are composite. 1 is neither prime nor composite.

**Co-prime**

Two numbers with **HCF = 1**. Need not be prime individually. E.g. (8, 9), (14, 15), (4, 9). Any two consecutive integers are always co-prime.

**Twin Prime**

Prime pairs differing by 2. E.g. (3,5), (5,7), (11,13), (17,19), (29,31), (41,43). The pair (2,3) is NOT twin prime (differ by 1).

**Even / Odd**

Even: divisible by 2 – (0, 2, 4, 6...). Odd: not divisible by 2 – (1, 3, 5...). Key: Odd + Odd = Even. Even  $\times$  Odd = Even. Odd  $\times$  Odd = Odd. Zero is even.

**Topic B****Place Value vs Face Value**

AFCAT Direct

**Face Value**

The **digit itself**, regardless of its position. Face value of 7 in 3,7,452 = 7. Face value never changes with position.

**Place Value**

The value of a digit based on its **position** in the number. In 3,7,452 – place value of 7 =  $7 \times 1,000 = 7,000$ .

**Example**

Number: 85,634

8  $\rightarrow$  place value = 80,000, face value = 8

5  $\rightarrow$  place value = 5,000, face value = 5

6  $\rightarrow$  place value = 600, face value = 6

3  $\rightarrow$  place value = 30, face value = 3

4  $\rightarrow$  place value = 4, face value = 4

Key: Place value = Face value  $\times$  Position value (ones=1, tens=10, hundreds=100...)

AFCAT Trap

Q: "What is the difference between place value and face value of 6 in 46,821?"

Place value of 6 = 6,000. Face value = 6. Difference = 6,000 - 6 = 5,994.

## HCF & LCM

## 2. HCF & LCM

FIG 2.1 — HCF VS LCM: KEY DIFFERENCES

### HCF — Highest Common Factor

Also called GCD or GCF

Take **LOWEST powers** of common primes

$$\text{HCF}(12,18): 12=2^2 \times 3, 18=2 \times 3^2$$

$$\rightarrow \text{HCF} = 2 \times 3 = 6$$

Divides both numbers exactly

$$\text{HCF} \leq \text{smaller of the two numbers}$$

### LCM — Lowest Common Multiple

Smallest number divisible by both

Take **HIGHEST powers** of all primes

$$\text{LCM}(12,18): 12=2^2 \times 3, 18=2 \times 3^2$$

$$\rightarrow \text{LCM} = 2^2 \times 3^2 = 36$$

Is a multiple of both numbers

$$\text{LCM} \geq \text{larger of the two numbers}$$

★ KEY FORMULA:  $\text{HCF} \times \text{LCM} = A \times B$  | Always verify with this!

### HCF Applications

- ▶ **Largest tile/piece:** Find HCF of dimensions (e.g., largest square tile for a 12 $\times$ 18 room =  $\text{HCF}(12,18) = 6$  m)
- ▶ **Largest number that divides:** HCF of the numbers

### LCM Applications

- ▶ **Events repeating together:** LCM of their periods (e.g., bells ringing every 4 and 6 min:  $\text{LCM} = 12$  min)
- ▶ **Smallest number divisible by both:** LCM of the numbers

- ▶ **Distribute into equal groups:** HCF gives max group size
- ▶ If HCF of  $a, b = H$ , then  $a = Hx, b = Hy$  where  $\text{HCF}(x,y) = 1$

- ▶ **Least time/distance:** Real-life scheduling problems
- ▶ LCM of co-prime numbers = their product

### ✂ Worked Example — HCF Real-Life: Largest Tile Size

A room is  $12\text{ m} \times 8\text{ m}$ . Find the largest square tile that can cover the floor exactly (no cutting).

The tile side must divide both 12 and 8 exactly.

$$\text{HCF}(12, 8): 12 = 2^2 \times 3, \quad 8 = 2^3$$

$$\text{HCF} = 2^2 = \mathbf{4\text{ m}}$$

$$\text{Number of tiles} = (12 \times 8) / (4 \times 4) = 96/16 = \mathbf{6\text{ tiles}}$$

✓ **Largest tile side = 4 m | Tiles needed = 6**

### ✂ Worked Example — LCM: Bells Tolling Together

Three bells toll at intervals of 9, 12 and 15 minutes. If they toll together at 8:00 AM, when will they next toll together?

**Step 1:** Find  $\text{LCM}(9, 12, 15)$

$$9 = 3^2 \quad 12 = 2^2 \times 3 \quad 15 = 3 \times 5$$

$$\text{LCM} = 2^2 \times 3^2 \times 5 = 4 \times 9 \times 5 = \mathbf{180\text{ minutes} = 3\text{ hours}}$$

**Step 2:** 8:00 AM + 3 hours = **11:00 AM**

✓ **Answer: 11:00 AM**

## SIMPLIFICATION & BODMAS

# 3. Simplification & BODMAS

FIG 3.1 — BODMAS ORDER OF OPERATIONS

**B****Brackets** $() [] \{ \}$ ① **First****O****Orders**

Powers, Roots

② **Second****D****Division**

÷

③ **Equal****M****Multiply**

×

③ **Equal****A****Addition**

+

④ **Equal****S****Subtract**

-

④ **Equal**

**D & M are EQUAL priority** — go left to right

e.g.  $8 \div 2 \times 4 = 4 \times 4 = 16$  (not 1)

**A & S are EQUAL priority** — go left to right

e.g.  $10 - 3 + 2 = 7 + 2 = 9$  (not 5)

💡 **BODMAS Key Rule:** D and M have equal priority — go **left to right**. Same for A and S. Brackets order: **( ) first, then [ ], then { }**. Never skip a step in AFCAT MCQs — always work innermost brackets outward.

### ✂ Worked Example — BODMAS

Simplify:  $18 \div 3 \times \{5 + [4 - (2 + 1)]\} - 2^2$

Step 1 (Inner bracket):  $(2+1) = 3$

Step 2 [Square bracket]:  $[4-3] = 1$

Step 3 {Curly bracket}:  $\{5+1\} = 6$

Step 4 (Orders):  $2^2 = 4$

Step 5 (D&M left to right):  $18 \div 3 = 6$ , then  $6 \times 6 = 36$

Step 6 (A&S):  $36 - 4 = 32$

✓ **Answer: 32**

## DECIMAL FRACTIONS & RECURRING DECIMALS

### 4. Decimal Fractions & Recurring Decimals

Type	Definition	Examp le	Fraction Form
Terminating Decimal	Ends after finite digits	0.75, 1.25, 0.5	$3/4, 5/4, 1/2$

Type	Definition	Example	Fraction Form
Pure Recurring	All digits after decimal repeat	$0.333\bar{3} = 0.\underline{3}$	Numerator = repeating block; Denominator = 9s equal to block length e.g. $0.\underline{3} = 3/9 = 1/3$
Mixed Recurring	Some digits fixed, rest repeat	$0.166\bar{6} = 0.1\underline{6}$	(Number - Non-repeating) ÷ (9s for repeat, 0s for non-repeat) e.g. $0.1\underline{6} = (16-1)/90 = 15/90 = 1/6$

### Recurring Decimal Formula:

Pure recurring:  $0.\underline{ab} = ab / 99$      $0.\underline{abc} = abc / 999$

Mixed recurring:  $0.\underline{xy} = (xy - x) / 90$      $0.x\underline{yz} = (xyz - xy) / 900$

## APPROXIMATION & ROUNDING

# 5. Approximation & Rounding Off

### 12 34 Rounding Rules

- ▶ **Rounding to nearest 10:** Look at units digit. If  $\geq 5 \rightarrow$  round up; if  $< 5 \rightarrow$  round down.  
E.g.  $47 \rightarrow 50$  |  $43 \rightarrow 40$
- ▶ **Rounding to nearest 100:** Look at tens digit. If  $\geq 5 \rightarrow$  round up.  
E.g.  $867 \rightarrow 900$  |  $832 \rightarrow 800$
- ▶ **Rounding to decimal places:** Look at the next digit after required place.  
E.g.  $3.456$  to 2 d.p.  $\rightarrow 3.46$  |  $3.453$  to 2 d.p.  $\rightarrow 3.45$
- ▶ **Significant figures:** Count from first non-zero digit.

### 12 34 Approximation in AFCAT

- ▶ **Approximate first, eliminate options:** If  $497 \times 203 \approx 500 \times 200 = 1,00,000 \rightarrow$  exact answer near 1,00,000
- ▶ **Square roots (approximate):**  $\sqrt{50} \approx 7.07$  |  $\sqrt{200} \approx 14.14$  |  $\sqrt{10} \approx 3.16$
- ▶ **When to round up:** When purchasing material (always buy more, not less)
- ▶ **When to round down:** When distributing items evenly (floor the value)

0.00427 to 2 sig. fig. = 0.0043

- ▶ AFCAT uses approximation to test whether students can estimate quickly without a calculator

### Worked Example — Approximation

Approximate:  $4,998 \times 52 \div 25.03$  (choose nearest from: 9,990 / 10,400 / 10,000 / 9,600)

Round each value:  $4,998 \approx 5,000$  |  $52 \approx 50$  |  $25.03 \approx 25$

$5,000 \times 50 \div 25 = 2,50,000 \div 25 = 10,000$

✓ Answer  $\approx 10,000$

## Formula Sheet — NA01

### HCF & LCM

$$\text{HCF} \times \text{LCM} = A \times B$$

HCF: take **lowest** powers of common primes

LCM: take **highest** powers of all primes

Co-prime: HCF = 1; LCM =  $A \times B$

### Number Types

Smallest prime: **2** (only even prime)

1 is **neither prime nor composite**

Twin primes: differ by **2**

Co-prime: HCF = **1**

### BODMAS Order

**B**rackets → **O**rders → **D**iv → **M**ul →  
**A**dd → **S**ub

D & M: left to right equally

A & S: left to right equally

Bracket order: ( ) → [ ] → { }

### Recurring Decimals

$$0.\underline{a} = a/9$$

$$0.\underline{ab} = ab/99$$

$$0.\underline{ab} = (ab-a)/90$$

$$0.\underline{abc} = (abc-ab)/900$$

### Divisibility Rules

By 2: last digit even

By 3: sum of digits  $\div 3$

### Squares & Cubes (Quick)

$$\sqrt{2} = 1.414 \quad \sqrt{3} = 1.732 \quad \sqrt{5} = 2.236$$

$$1^3=1, 2^3=8, 3^3=27, 4^3=64, 5^3=125$$

By 4: last 2 digits  $\div 4$   
By 9: sum of digits  $\div 9$   
By 11: (sum odd – sum even)  $\div 11$

$6^3=216$ ,  $7^3=343$ ,  $8^3=512$ ,  $9^3=729$ ,  
 $10^3=1000$   
 $\sqrt[3]{512}=8$ ,  $\sqrt[3]{729}=9$ ,  $\sqrt[3]{1000}=10$

## Topic-Wise PYQs – NAO1

**Q1. The HCF of 36 and 84 is:** AFCAT PYQ

(a) 6 (b) 12 (c) 18 (d) 24

✓ Answer: (b) 12

$36 = 2^2 \times 3^2$  |  $84 = 2^2 \times 3 \times 7$ . HCF =  $2^2 \times 3 = 12$ . (Take lowest powers of common primes.)

**Q2. LCM of 12, 18 and 24 is:** AFCAT PYQ

(a) 36 (b) 48 (c) 72 (d) 144

✓ Answer: (c) 72

$12=2^2 \times 3$  |  $18=2 \times 3^2$  |  $24=2^3 \times 3$ . LCM =  $2^3 \times 3^2 = 8 \times 9 = 72$ .

**Q3. Simplify:  $5 + 3 \times 4 - 12 \div 3$**  AFCAT PYQ

(a) 13 (b) 9 (c) 17 (d) 28

✓ Answer: (a) 13

BODMAS:  $12 \div 3 = 4$ ;  $3 \times 4 = 12$ ; then  $5 + 12 - 4 = 13$ . Common mistake: doing  $5+3$  first.

**Q4. 0.36 as a fraction is:** ⚡ Tricky

(a)  $36/99$  (b)  $4/11$  (c)  $9/25$  (d)  $36/100$

✓ Answer: (b)  $4/11$

Pure recurring  $0.\underline{36}$  =  $36/99 = 4/11$ . (Two repeating digits  $\rightarrow$  denominator = 99.)

**Q5. Which of the following is NOT a prime number?** AFCAT PYQ

(a) 89 (b) 97 (c) 91 (d) 83

✓ Answer: (c) 91

91 = 7 × 13. Not prime. 83, 89, 97 are all prime. Quick check: try dividing by primes up to  $\sqrt{91} \approx 9.5$ , so check 2,3,5,7 only.

**Q6. If HCF of two numbers is 8 and their LCM is 96, and one number is 32, the other is:** AFCAT PYQ

(a) 16 (b) 24 (c) 48 (d) 64

✓ Answer: (b) 24

HCF × LCM = A × B → 8 × 96 = 32 × B → B = 768/32 = 24.

## 🧠 Quick Memory Chart — NAO1

### Number Types

- ◆ Smallest prime: **2**
- ◆ Only even prime: **2**
- ◆ 1 = **neither prime/composite**
- ◆ Twin primes: **differ by 2**
- ◆ Co-prime: **HCF = 1**
- ◆ 0 is **even, whole, not natural**

### HCF & LCM

- ◆ HCF: **lowest powers** (common)
- ◆ LCM: **highest powers** (all)
- ◆ **HCF × LCM = A × B**
- ◆ Co-prime: LCM = **A × B**
- ◆ HCF always **divides** LCM
- ◆ LCM ≥ HCF always

### BODMAS

- ◆ B → O → D → M → A → S
- ◆ D & M: **left to right**
- ◆ A & S: **left to right**
- ◆ Bracket: **() [] {}**
- ◆ Square root: **Order (O)**
- ◆ Always innermost first

 Mock Tests

 Subject Quiz

 Telegram

